

*Wolf Scheuermann / Navigation*

# TCAS / TCAD Logic

- ✓ Protected Volume of Airspace
- ✓ Demonstration of Properties and Limits

# Why about Protected Volume?

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- ✓ To show how this Protected Volume of airspace is generated by the software algorithms.
- ✓ To enhance the knowledge about its properties and its behavior.
- ✓ To demonstrate its limits.

# TCAS / TCAD

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✓ Traffic Alert & Collision Avoidance System (TCAS):

- *Traffic Alert (TA)*
- *Resolution Advisory (RA)*  
vertical maneuvres only

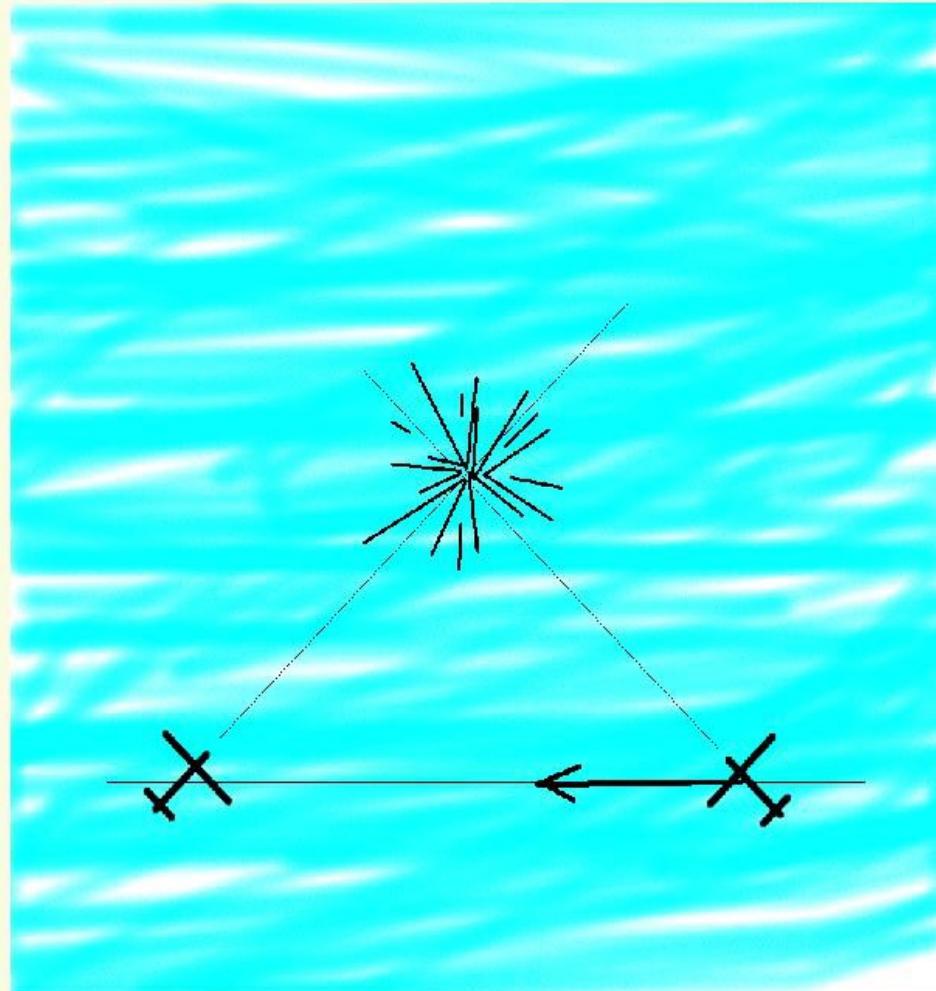
✓ Traffic Collision Alerting Device (TCAD):

- *Traffic Alert (TA)*

# Collision Situation

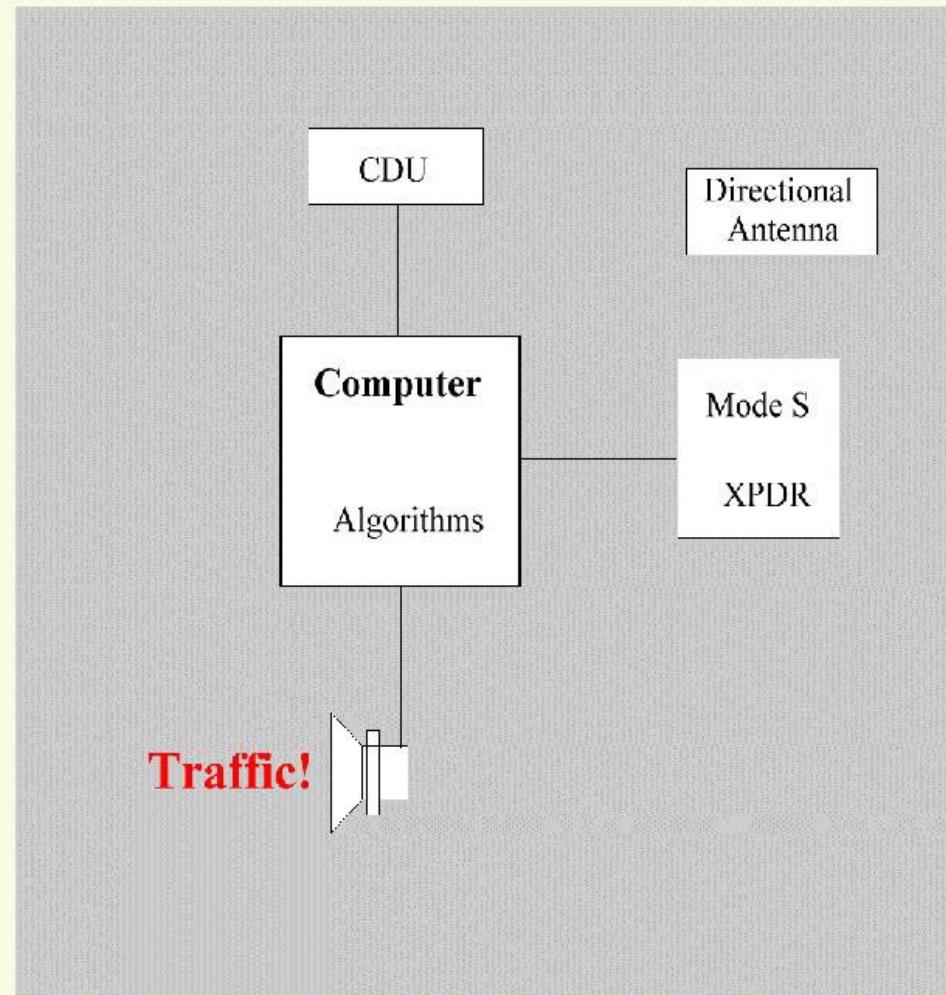
- ✓ Own A/C
- ✓ Intruder
- ✓ Fixed Bearing
- ✓ Range decreasing
- ✓ **COLLISION!**

*Collision Plane*



# TCAS / TCAD *System Components*

- ✓ Computer
- ✓ Software Algorithms
- ✓ Directional Antenna
- ✓ Mode S Transponder
- ✓ Control & Display Unit (CDU)
- ✓ Speaker



# Measurements

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- ✓ Surveillance Volume: 40 NM
- ✓ Alert Time (TA) at average altitudes:  $\tau = 40$  sec
- ✓ Alert Time (RA) at average altitudes:  $\tau = 25$  sec

## **Measured parameters of the intruder:**

- ✓ Range (r) & Altitude (Alt) & relative Direction

## **Calculated parameters of the intruder:**

- ✓ Range Rate ( $r'$ )
- ✓ Altitude difference to own A/C ( $\Delta$ Alt)

# Protected Volume

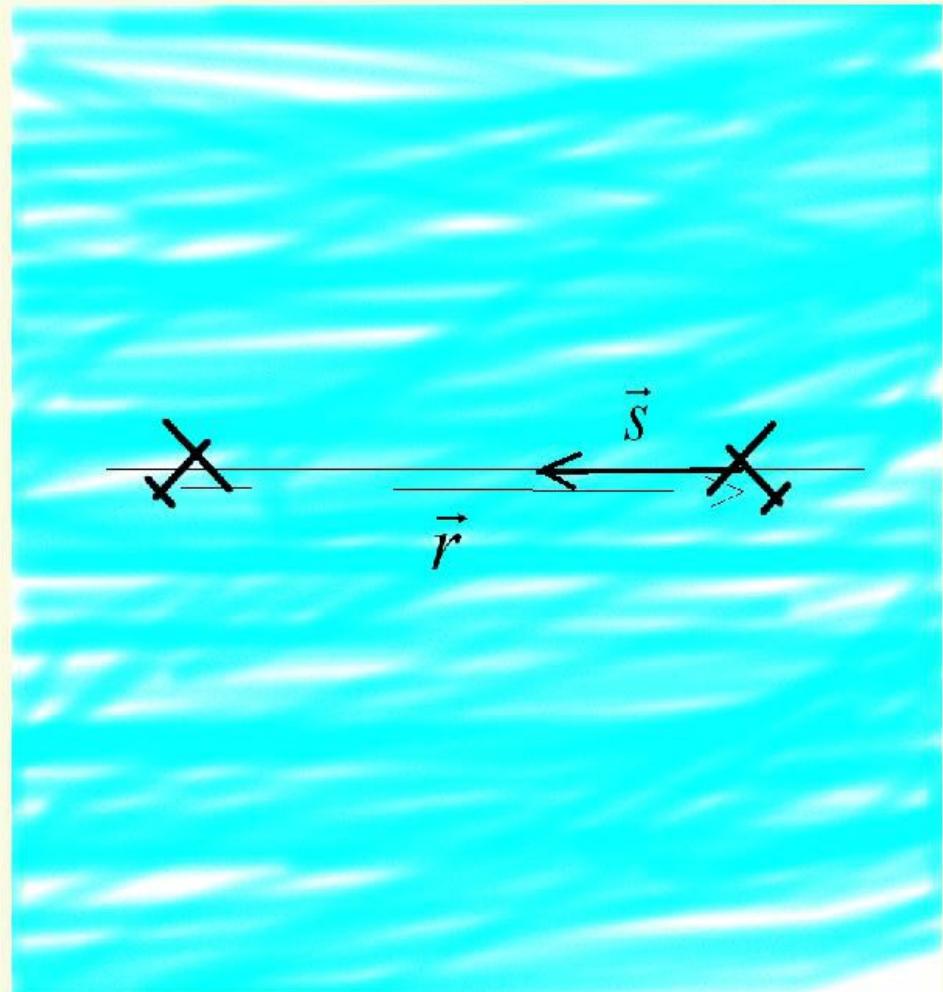
Part 1

## Collision Situation

- ✓ Range ( $\mathbf{r}$ )
- ✓ relative Speed ( $\mathbf{s}$ )

*Alert  $\tau$  sec before impact:*

$$\vec{r} = -\vec{s} \cdot \tau$$



# Protected Volume

*Part 2*

## Collision Situation

✓ Here

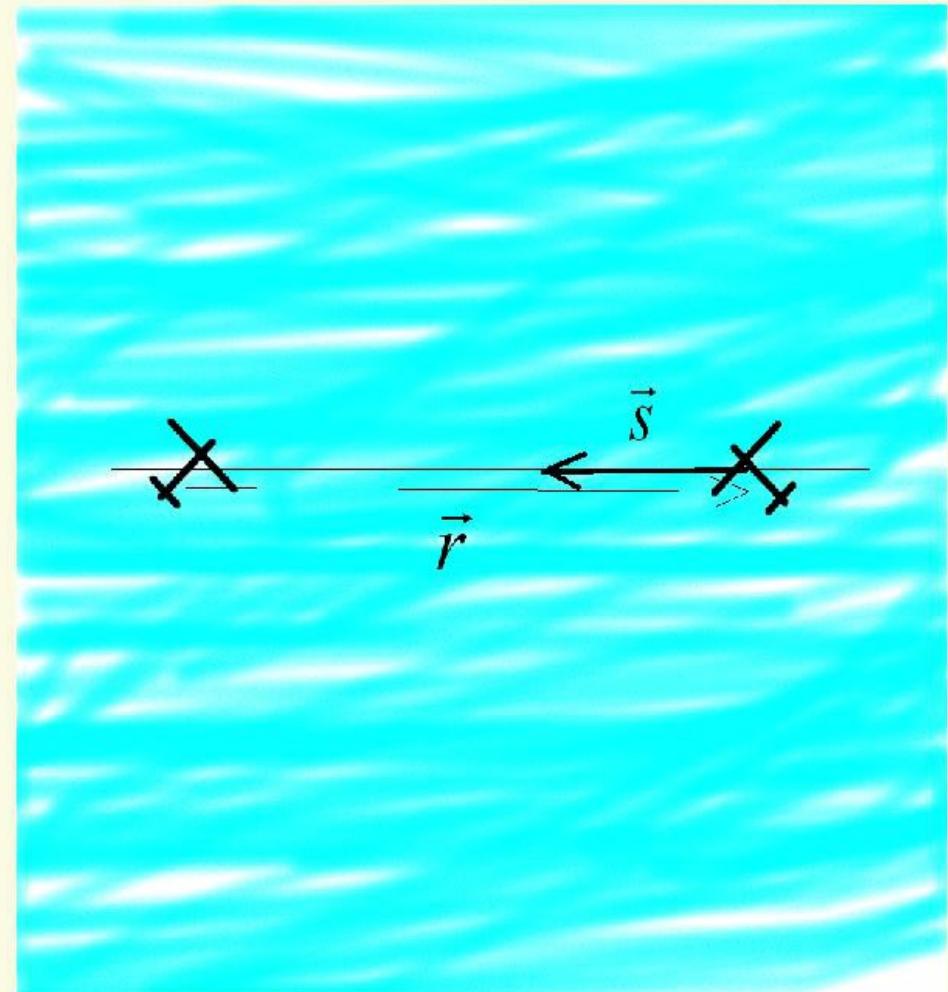
$$\vec{s} = \vec{r}$$

✓ Therefore

$$\tau = -\frac{\vec{r}}{\dot{\vec{r}}}$$

( $\tau$  Criterion)

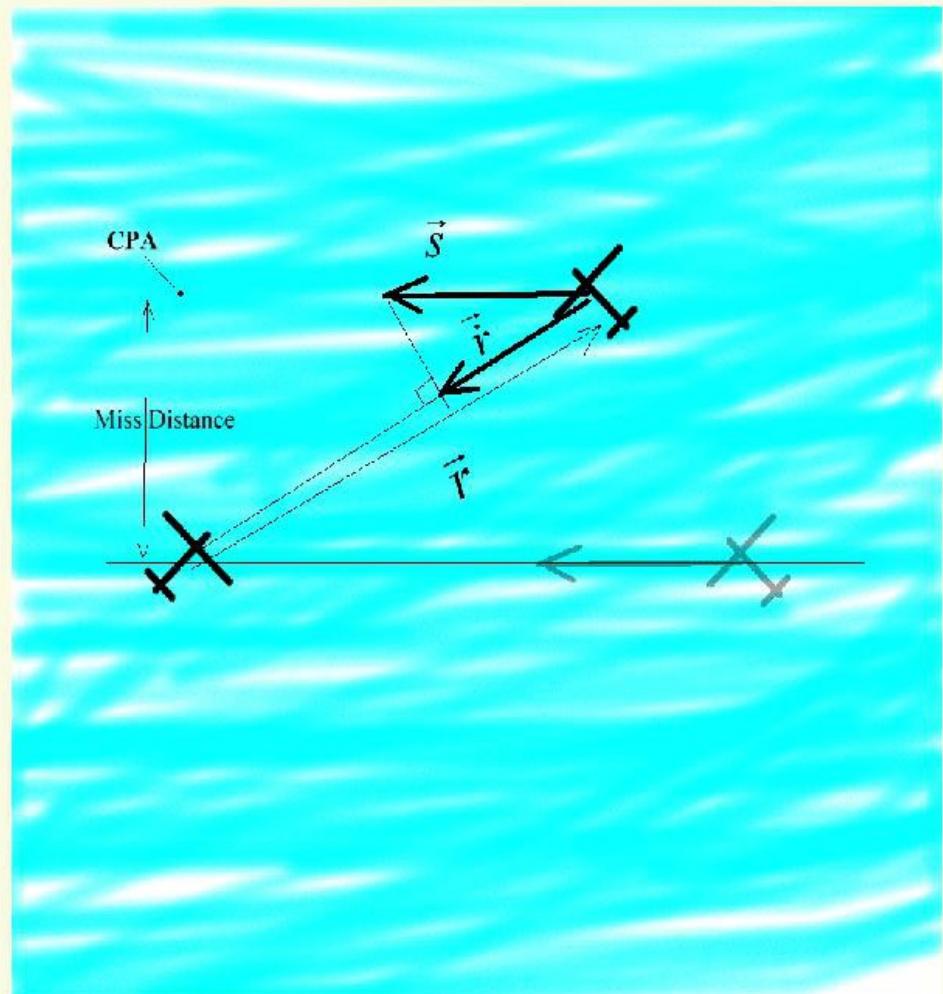
✓ RangeTest



# Near Miss

Part 1

- ✓ Same relative speed  $s$
- ✓ Miss distance
- ✓ Closest Point of Approach (CPA)
- ✓ Here  $\vec{s} \neq \vec{r}$
- ✓ How does the  $\tau$  criterion work here?



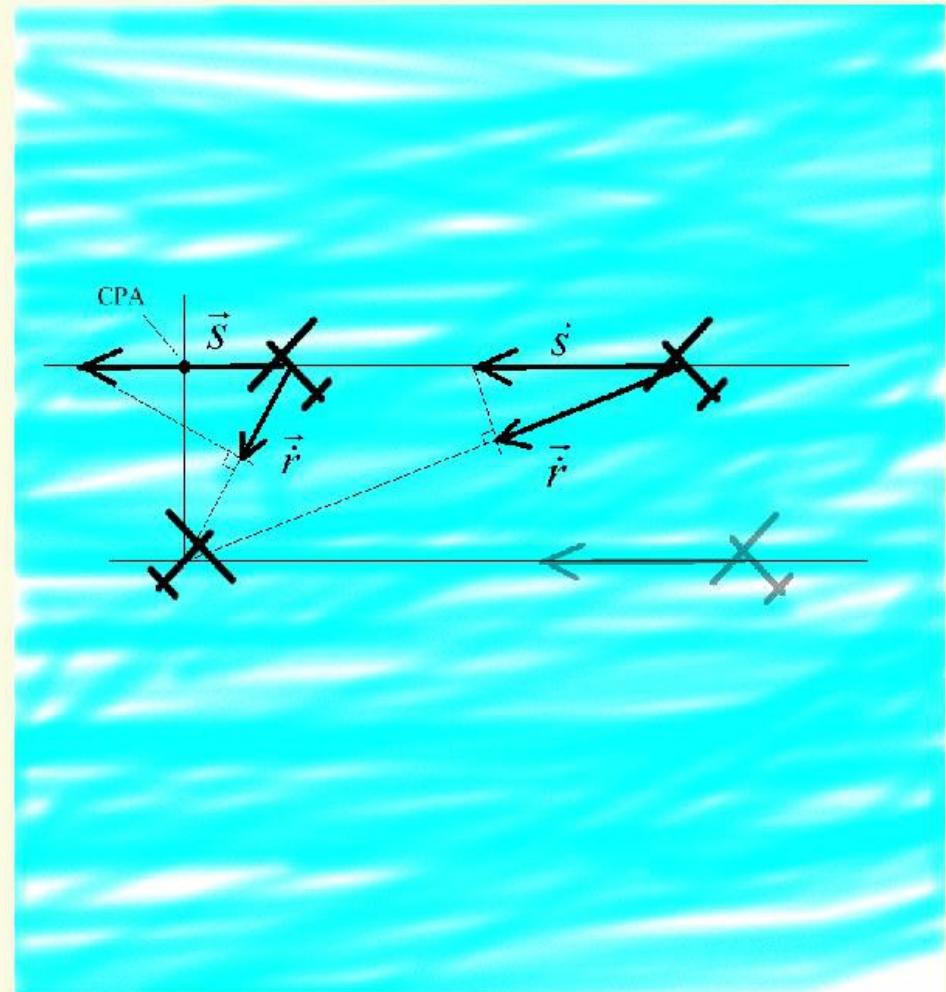
# Near Miss

Part 2

- ✓ While the relative speed  $s$  is constant the range rate  $\dot{r}'$  changes!
- ✓  $s$  is unknown (direction is necessary)!

*Alert will sound when:*

$$\tau = -\frac{\vec{r}}{\dot{\vec{r}}} \quad \text{or} \quad \vec{r} = -\dot{\vec{r}} \cdot \tau$$

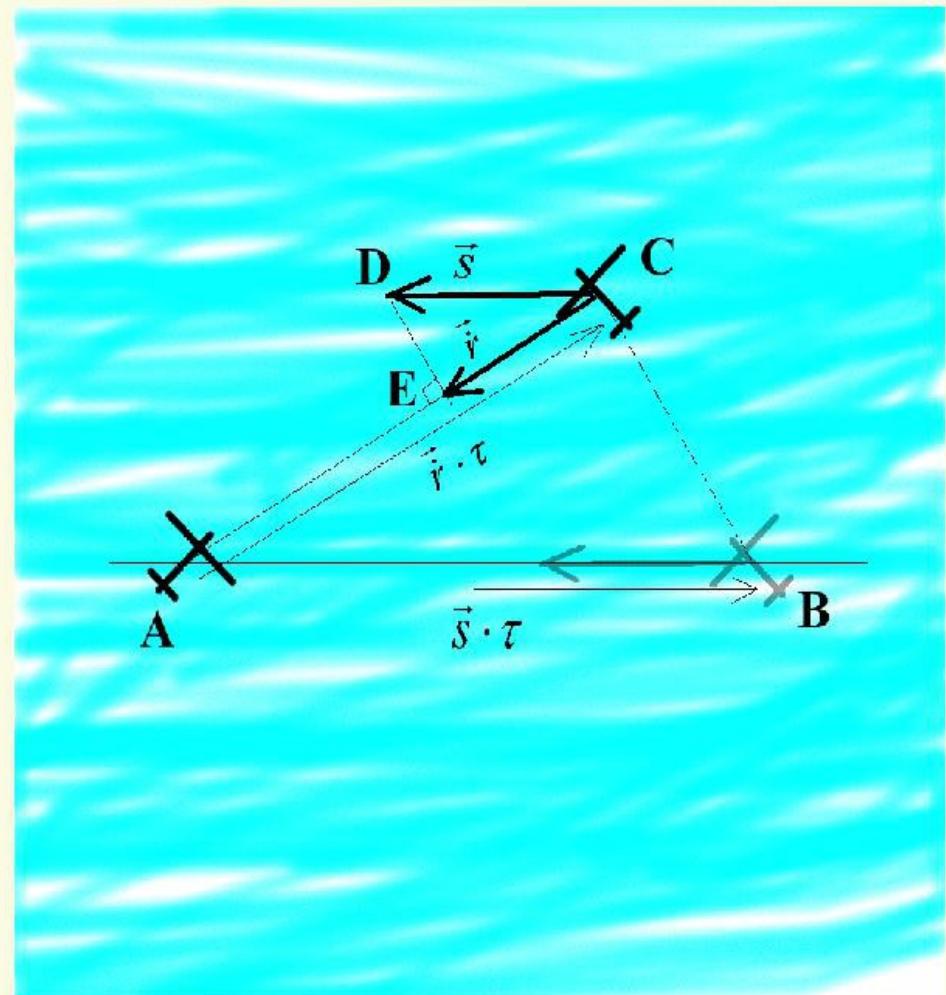


# Near Miss

## Part 3

- ✓ Whenever the intruder is in position B or C the alert will sound, because the  $\tau$  criterion is fulfilled!

*What do we know about the position C of the intruder when the alert sounds?*



# Near Miss

## Part 4

✓ Triangle CDE is rectangular!

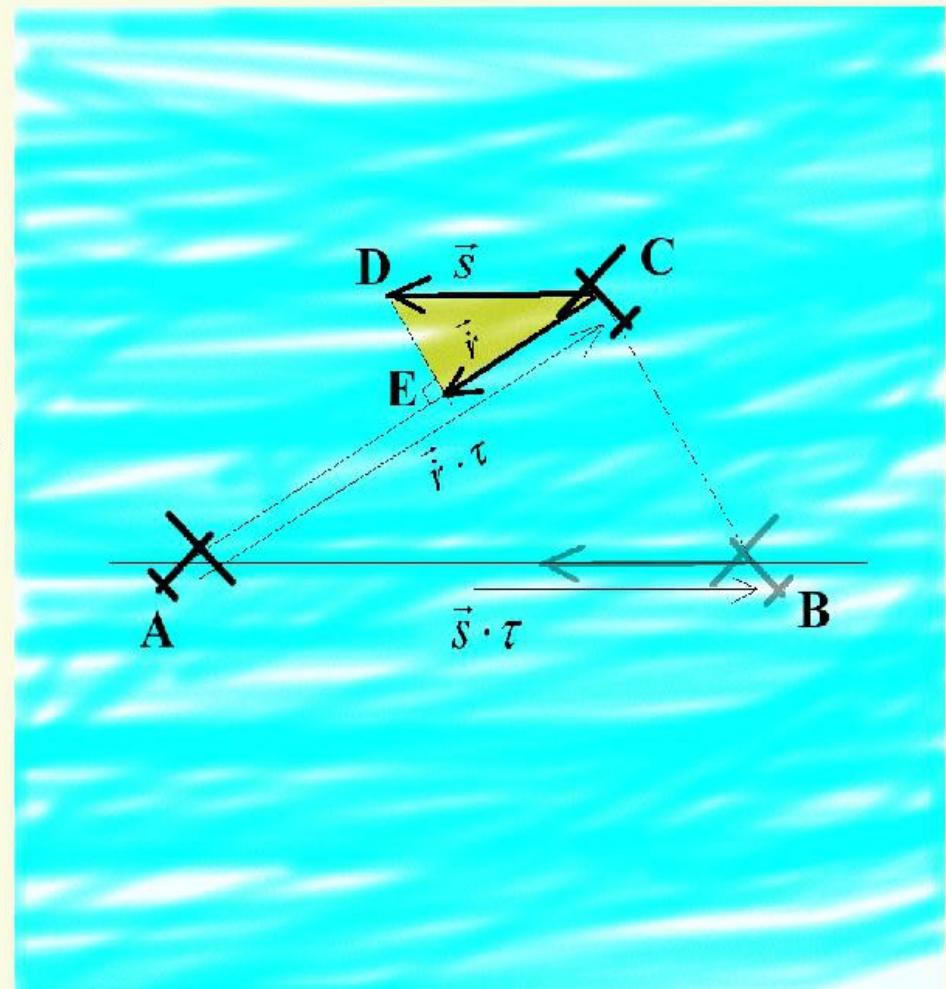
The relation between the side  $\vec{r}'$  and the hypotenuse  $\vec{s}$

$$\frac{\vec{r}}{\vec{s}} = \frac{\vec{r}}{\vec{s}} \cdot 1 = \frac{\vec{r}}{\vec{s}} \cdot \frac{\tau}{\tau} = \frac{\vec{r} \cdot \tau}{\vec{s} \cdot \tau}$$

... is the same as in the triangle ABC!

✓ Therefore:

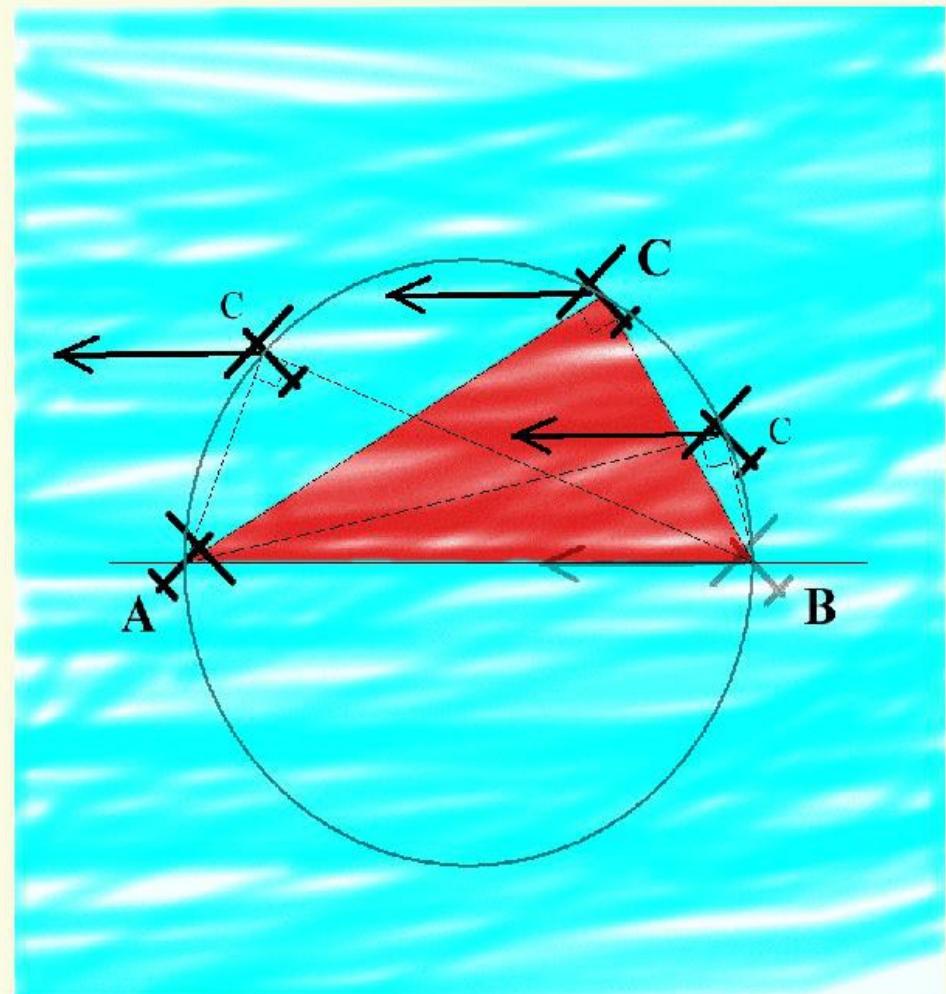
*Triangle ABC is also rectangular!*



# Near Miss

## Part 5

- ✓ The Alert sounds whenever the intruder is at the rectangular corner of the triangle ABC.
- ✓ This means: it is on a *Circle of Thales!*
- ✓ So: This circle is the *alarm boundary* of the  $\tau$  criterion!

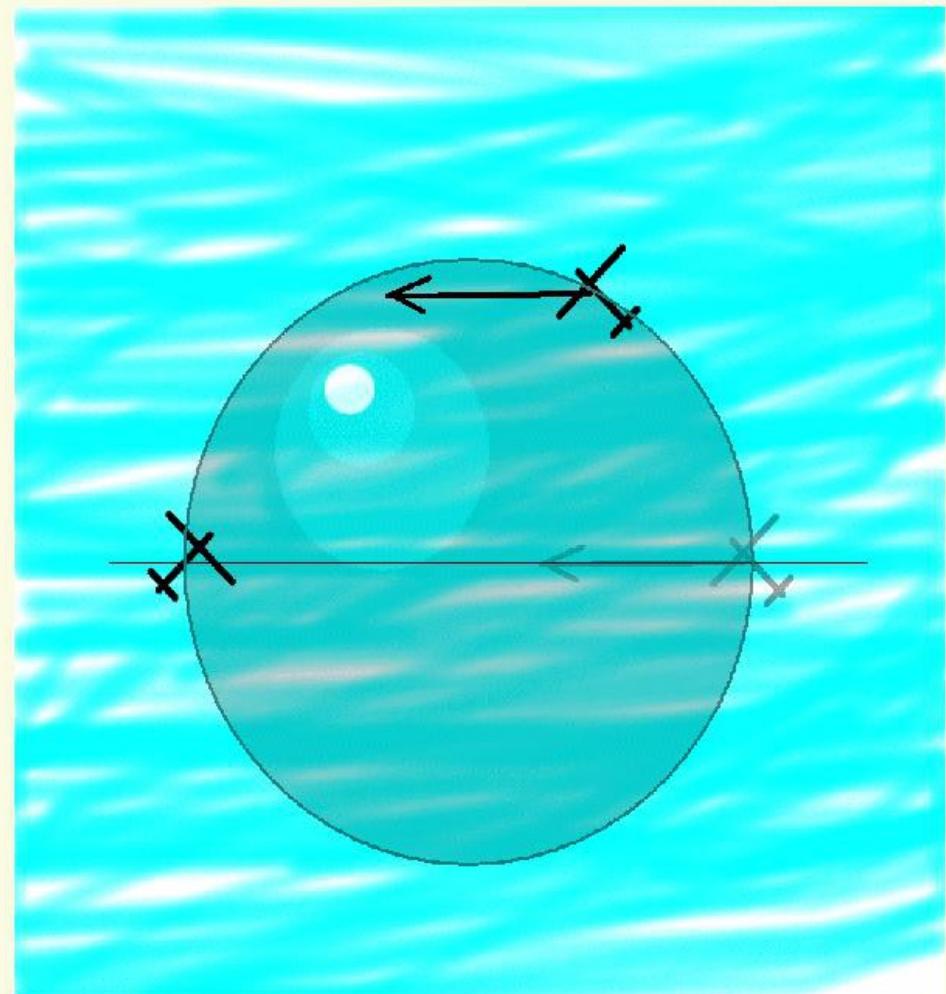


# Near Miss

## Part 6

- ✓ The Collision Plane is not necessarily horizontal: the alarm boundary is actually a **sphere**:

The *Protected Volume of Airspace*



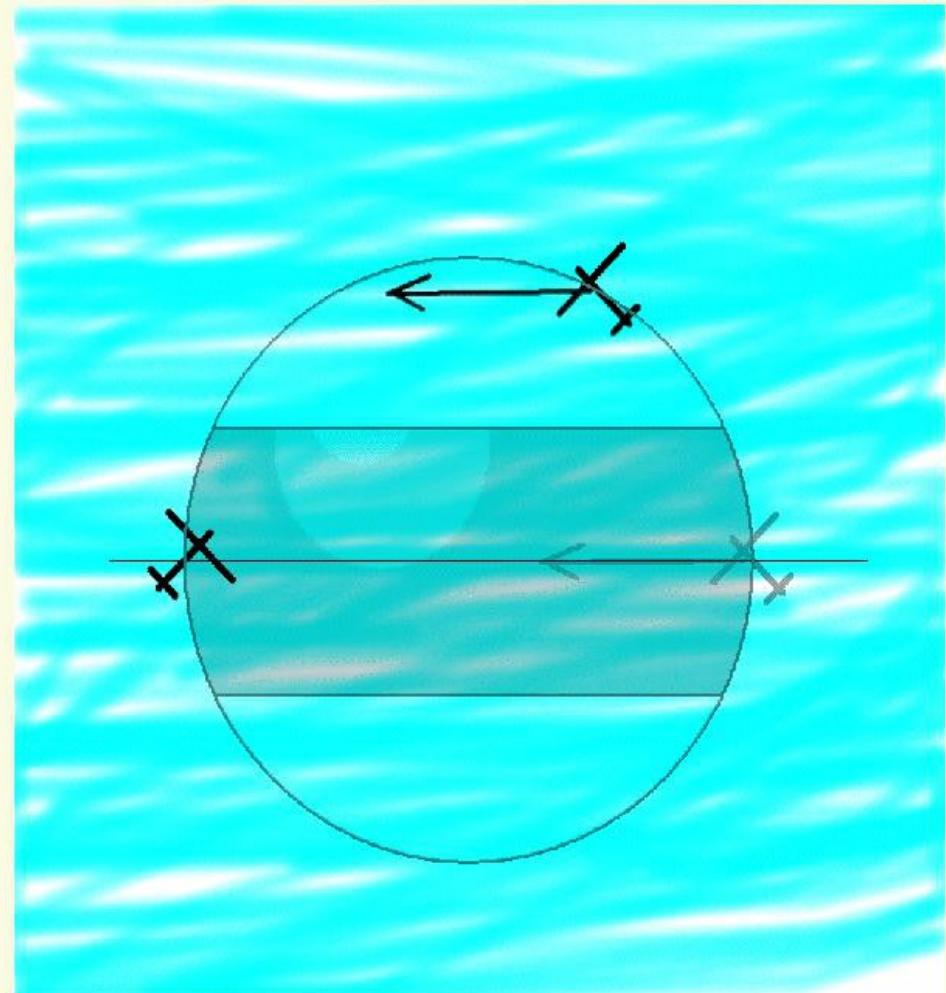
# Near Miss

Part 7

- ✓ Actually, this sphere is too large.
- ✓ A slice is cut out via a *Vertical  $\tau$  Criterion*.

## ✓ Altitude Test

- ✓ The intruder has to pass both the Range Test and the Altitude Test to trigger an alarm.

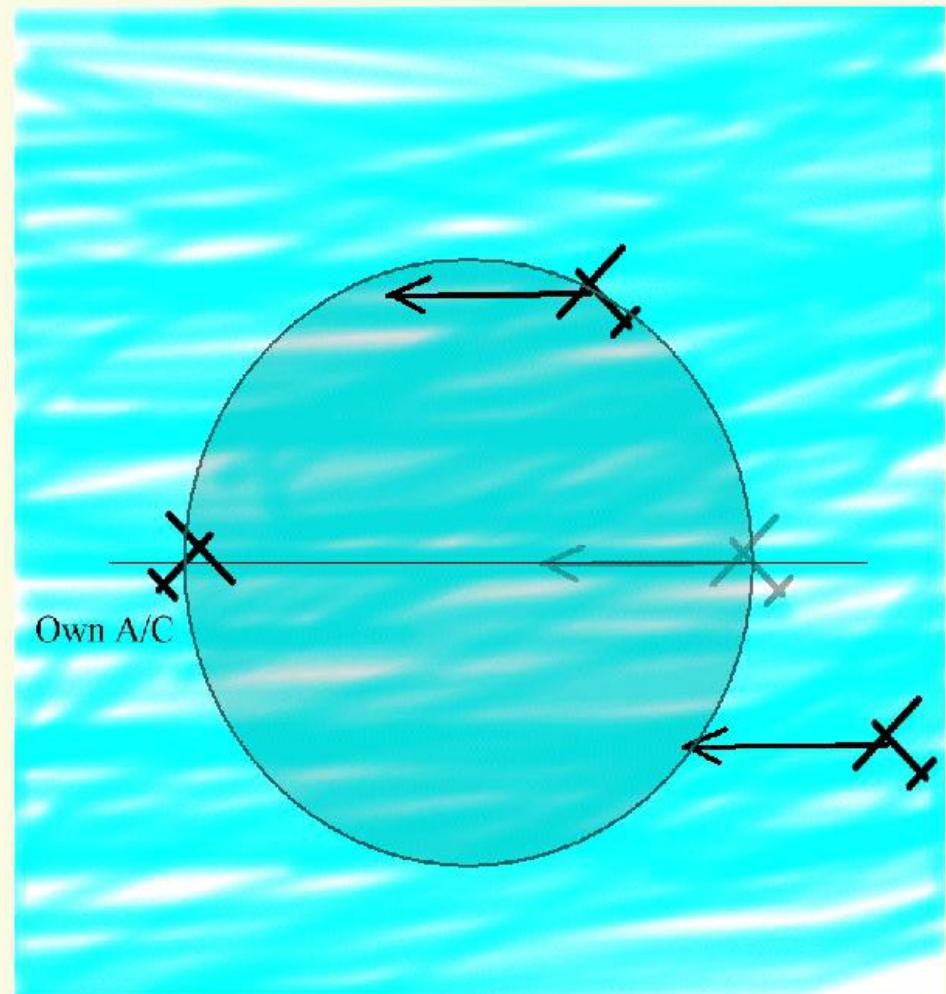


# Near Miss

*Part 8*

## Summary:

- ✓ The Protected Volume of Airspace is always **between** the aircrafts.
- ✓ Own A/C is **on the surface** of the sphere, not in the center.
- ✓ The Protected Volume is oriented **towards the relative motion** of the intruder.
- ✓ The **radius** depends on the relative speed.



# Protected Volume *Properties & Limits*

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- ✓ The *simple  $\tau$  Criterion* is not always safe
  - ... An intruder could come close without alert.
- ✓ A *Modified  $\tau$  Criterion* was developed
  - ... But caused too much nuisance alerts.
- ✓ Now the *New  $\tau$  Criterion* is implemented
  - ... Which avoids the former flaws.

# Protected Volume *Properties & Limits*

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- ✓ If an aircraft has no transponder it cannot be detected at all.
- ✓ The alert time  $\tau$  can deteriorate in some cases.
- ✓ Horizontal collision avoidance manoeuvres are difficult to program  
... and are sometimes tricky!

[Own Aircraft](#) [Intruder](#) [ICAS](#)**Simulation Time**

0 : 0 : 0

**OWN AIRCRAFT:**

TH = 000 \*

TAS = 150kt

**PROTECTED VOL.:**

Radius = 0.2 NM

Dmod = 0.5 NM

**INTRUDER:**

TH = 335 \*

TAS = 150kt

**Range:**

2.1 NM

**Range Rate:**

0 kt

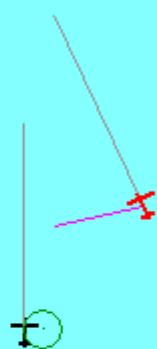
**Relative Speed:**

65 kt

CPA = 1.2 NM

TCPA = 0 : 1 : 34

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

**Beenden**

Own Aircraft Intruder ICAS



## Simulation Time

0 : 0 : 17

## OWN AIRCRAFT:

TH = 000 \*

TAS = 150kt

## PROTECTED VOL.:

Radius = 0.5 NM

Dmod = 0.5 NM

## INTRUDER:

TH = 305 \*

TAS = 150kt

## Range:

1.7 NM

## Range Rate:

0 kt

## Relative Speed:

139 kt

CPA = 0.7 NM

TCPA = 0 : 0 : 40

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

Beenden



[Own Aircraft](#) [Intruder](#) [ICAS](#)**Simulation Time**

0 : 0 : 26

**OWN AIRCRAFT:**

TH = 000 \*

TAS = 150kt

**PROTECTED VOL.:**

Radius = 0.8 NM

Dmod = 0.5 NM

**INTRUDER:**

TH = 265 \*

TAS = 150kt

**Range:**

1.3 NM

**Range Rate:**

0 kt

**Relative Speed:**

221 kt

CPA = 0.2 NM

TCPA = 0 : 0 : 21

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

**Beenden**

Own Aircraft Intruder ICAS



## Simulation Time

0 : 0 : 32

## OWN AIRCRAFT:

TH = 000 \*

TAS = 150kt

## PROTECTED VOL.:

Radius = 1 NM

Dmod = 0.5 NM

## INTRUDER:

TH = 200 \*

TAS = 150kt

## Range:

0.9 NM

## Range Rate:

0 kt

## Relative Speed:

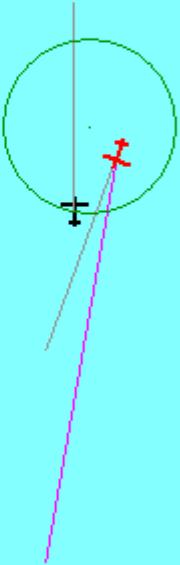
295 kt

CPA = 0.4 NM

TCPA = 0 : 0 : 9

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

Beenden



Own Aircraft   Intruder   ICAS



## Simulation Time

0 : 0 : 0

## OWN AIRCRAFT:

TH = 000 \*

TAS = 150kt

## PROTECTED VOL.:

Radius = 0.2 NM

Dmod = 0.5 NM

## INTRUDER:

TH = 335 \*

TAS = 150kt

## Range:

2.1 NM

## Range Rate:

0 kt

## Relative Speed:

65 kt

CPA = 1.2 NM

TCPA = 0 : 1 : 34

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

Beenden



[Own Aircraft](#) [Intruder](#) [ICAS](#)**Simulation Time**

0 : 0 : 0

**OWN AIRCRAFT:**

TH = 000 \*

TAS = 150kt

**PROTECTED VOL.:**

Radius = 0.7 NM

Dmod = 0.5 NM

**INTRUDER:**

TH = 280 \*

TAS = 150kt

## Range:

4.4 NM

## Range Rate:

0 kt

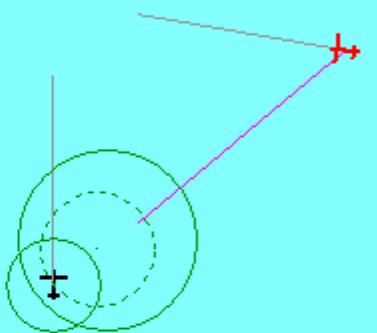
## Relative Speed:

193 kt

CPA = 0.1 NM

TCPA = 0 : 1 : 23

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

**Beenden**

[Own Aircraft](#) [Intruder](#) [ICAS](#)**Simulation Time**

0 : 0 : 0

**OWN AIRCRAFT:**

TH = 000 \*

TAS = 150kt

**PROTECTED VOL.:**

Radius = 0.7 NM

Dmod = 0.5 NM

**INTRUDER:**

TH = 280 \*

TAS = 150kt

## Range:

4.4 NM

## Range Rate:

0 kt

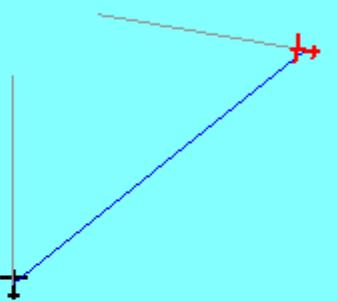
## Relative Speed:

193 kt

CPA = 0.1 NM

TCPA = 0 : 1 : 23

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

**Beenden**

[Own Aircraft](#) [Intruder](#) [ICAS](#)**Simulation Time**

0 : 0 : 7

**OWN AIRCRAFT:**

TH = 000 \*

TAS = 150kt

**PROTECTED VOL.:**

Radius = 0.7 NM

Dmod = 0.5 NM

**INTRUDER:**

TH = 280 \*

TAS = 150kt

**Range:**

4 NM

**Range Rate:**

-193 kt

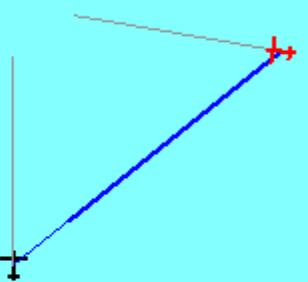
**Relative Speed:**

193 kt

CPA = 0.1 NM

TCPA = 0 : 1 : 16

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

**Beenden**

[Own Aircraft](#) [Intruder](#) [ICAS](#)**Simulation Time**

0 : 0 : 7

**OWN AIRCRAFT:**

TH = 000 \*

TAS = 150kt

**PROTECTED VOL.:**

Radius = 0.7 NM

Dmod = 0.5 NM

**INTRUDER:**

TH = 280 \*

TAS = 150kt

**Range:**

4 NM

**Range Rate:**

-193 kt

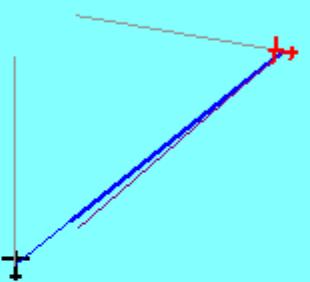
**Relative Speed:**

193 kt

CPA = 0.1 NM

TCPA = 0 : 1 : 16

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

**Beenden**

Own Aircraft Intruder TCAS



## Simulation Time

0 : 0 : 10

## OWN AIRCRAFT:

TH = 000 \*

TAS = 150kt

## PROTECTED VOL.:

Radius = 0.7 NM

Dmod = 0.5 NM

## INTRUDER:

TH = 280 \*

TAS = 150kt

## Range:

3.9 NM

## Range Rate:

0 kt

## Relative Speed:

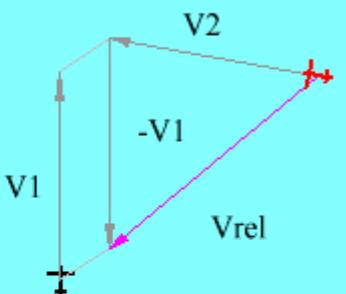
193 kt

CPA = 0.1 NM

TCPA = 0 : 1 : 13

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

Beenden



[Own Aircraft](#) [Intruder](#) [ICAS](#)**Simulation Time**

0 : 0 : 10

**OWN AIRCRAFT:**

TH = 000 \*

TAS = 150kt

**PROTECTED VOL.:**

Radius = 0.7 NM

Dmod = 0.5 NM

**INTRUDER:**

TH = 280 \*

TAS = 150kt

## Range:

3.9 NM

## Range Rate:

0 kt

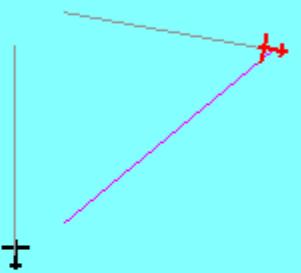
## Relative Speed:

193 kt

CPA = 0.1 NM

TCPA = 0 : 1 : 13

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

**Beenden**

Own Aircraft Intruder ICAS



## Simulation Time

0 : 0 : 44

## OWN AIRCRAFT:

TH = 000 \*

TAS = 150kt

## PROTECTED VOL.:

Radius = 0.7 NM

Dmod = 0.5 NM

## INTRUDER:

TH = 280 \*

TAS = 150kt

## Range:

2.1 NM

## Range Rate:

0 kt

## Relative Speed:

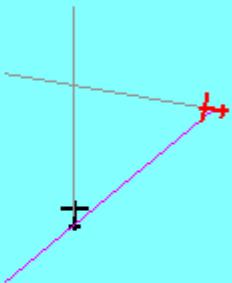
193 kt

CPA = 0.1 NM

TCPA = 0 : 0 : 39

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

Beenden



Own Aircraft   Intruder   ICAS



## Simulation Time

0 : 0 : 0

## OWN AIRCRAFT:

TH = 000 \*

TAS = 150kt

## PROTECTED VOL.:

Radius = 0.7 NM

Dmod = 0.5 NM

## INTRUDER:

TH = 280 \*

TAS = 150kt

## Range:

2.2 NM

## Range Rate:

0 kt

## Relative Speed:

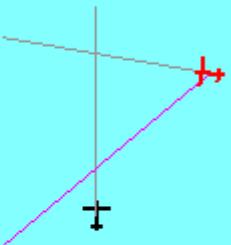
193 kt

CPA = 0.4 NM

TCPA = 0 : 0 : 39

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

Beenden



Own Aircraft Intruder ICAS



## Simulation Time

0 : 0 : 0

## OWN AIRCRAFT:

TH = 000 \*

TAS = 150kt

## PROTECTED VOL.:

Radius = 0.7 NM

Dmod = 0.5 NM

## INTRUDER:

TH = 280 \*

TAS = 150kt

## Range:

2.2 NM

## Range Rate:

0 kt

## Relative Speed:

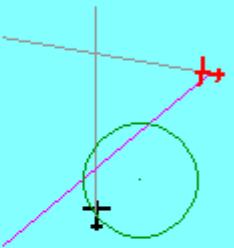
193 kt

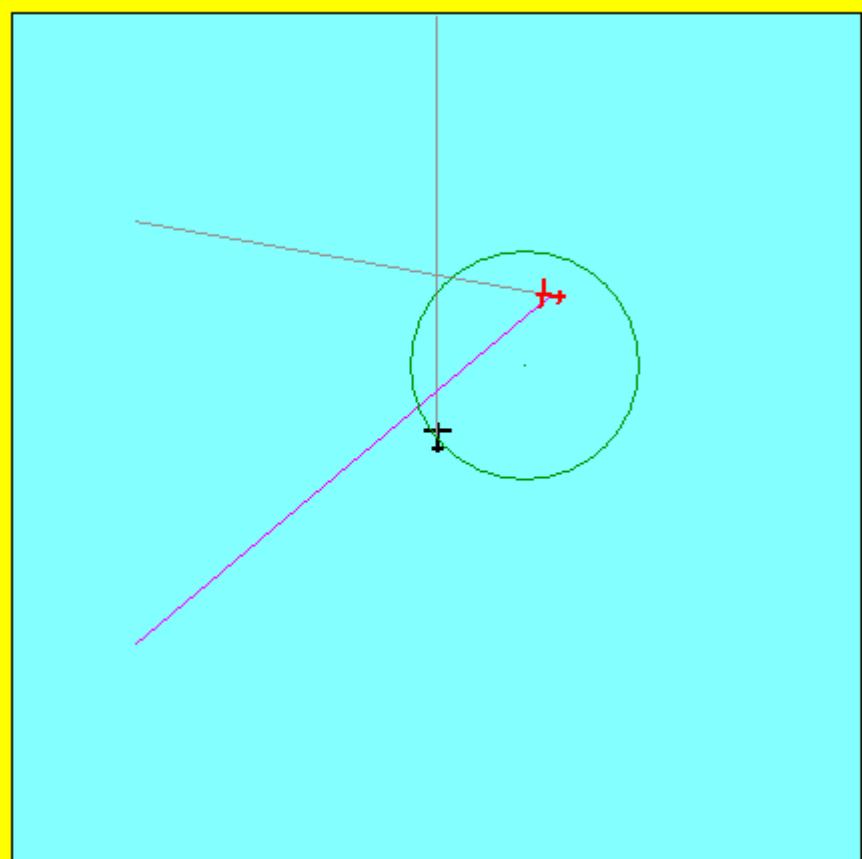
CPA = 0.4 NM

TCPA = 0 : 0 : 39

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

Beenden



[Own Aircraft](#) [Intruder](#) [ICAS](#)**Simulation Time**

0 : 0 : 0

**OWN AIRCRAFT:**

TH = 000 \*

TAS = 300kt

**PROTECTED VOL.:**

Radius = 1.3 NM

Dmod = 0.5 NM

**INTRUDER:**

TH = 280 \*

TAS = 300kt

**Range:**

2.2 NM

**Range Rate:**

0 kt

**Relative Speed:**

386 kt

CPA = 0.4 NM

TCPA = 0 : 0 : 20

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

**Beenden**

Own Aircraft Intruder ICAS



## Simulation Time

0 : 0 : 0

## OWN AIRCRAFT:

TH = 000 \*

TAS = 150kt

## PROTECTED VOL.:

Radius = 0.7 NM

Dmod = 0.5 NM

## INTRUDER:

TH = 280 \*

TAS = 150kt

## Range:

2.2 NM

## Range Rate:

0 kt

## Relative Speed:

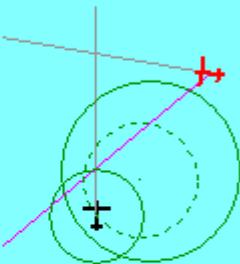
193 kt

CPA = 0.4 NM

TCPA = 0 : 0 : 39

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

Beenden



Own Aircraft Intruder ICAS



## Simulation Time

0 : 0 : 0

## OWN AIRCRAFT:

TH = 000 \*

TAS = 150kt

## PROTECTED VOL.:

Radius = 0.9 NM

Dmod = 0.5 NM

## INTRUDER:

TH = 280 \*

TAS = 150kt

## Range:

2.2 NM

## Range Rate:

0 kt

## Relative Speed:

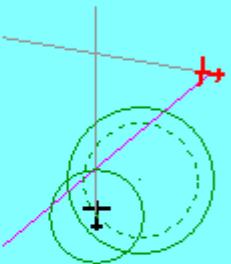
193 kt

CPA = 0.4 NM

TCPA = 0 : 0 : 39

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

Beenden



[Own Aircraft](#) [Intruder](#) [ICAS](#)**Simulation Time**

0 : 0 : 0

**OWN AIRCRAFT:**

TH = 000 \*

TAS = 150kt

**PROTECTED VOL.:**

Radius = 0 NM

Dmod = 0.5 NM

**INTRUDER:**

TH = 15 \*

TAS = 120kt

**Range:**

2.4 NM

**Range Rate:**

0 kt

**Relative Speed:**

46 kt

CPA = 0.1 NM

TCPA = 0 : 3 : 7

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

**Beenden**

[Own Aircraft](#) [Intruder](#) [ICAS](#)**Simulation Time**

0 : 0 : 0

**OWN AIRCRAFT:**

TH = 000 \*

TAS = 150kt

**PROTECTED VOL.:**

Radius = 0 NM

Dmod = 0.5 NM

**INTRUDER:**

TH = 30 \*

TAS = 120kt

**Range:**

2.4 NM

**Range Rate:**

0 kt

**Relative Speed:**

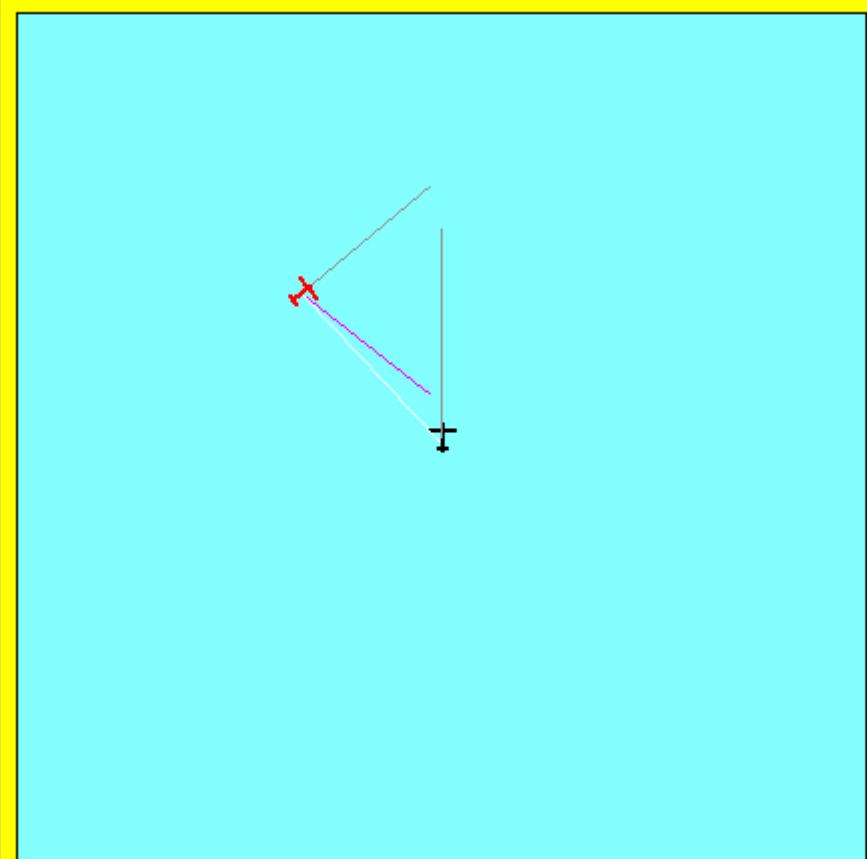
76 kt

CPA = 0.3 NM

TCPA = 0 : 1 : 53

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

**Beenden**

[Own Aircraft](#) [Intruder](#) [ICAS](#)**Simulation Time**

0 : 0 : 0

**OWN AIRCRAFT:**

TH = 000 °

TAS = 150kt

**PROTECTED VOL.:**

Radius = 0 NM

Dmod = 0.5 NM

**INTRUDER:**

TH = 50 °

TAS = 120kt

**Range:**

2.4 NM

**Range Rate:**

0 kt

**Relative Speed:**

117 kt

CPA = 0.3 NM

TCPA = 0 : 1 : 13

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

**Beenden**

[Own Aircraft](#) [Intruder](#) [ICAS](#)**Simulation Time**

0 : 0 : 0

**OWN AIRCRAFT:**

TH = 000 \*

TAS = 150kt

**PROTECTED VOL.:**

Radius = 0 NM

Dmod = 0.5 NM

**INTRUDER:**

TH = 70 \*

TAS = 120kt

**Range:**

2.4 NM

**Range Rate:**

0 kt

**Relative Speed:**

157 kt

CPA = 0.1 NM

TCPA = 0 : 0 : 55

- Fliegen
- Range
- Range Rate
- TAS
- V relative
- Protected Vol.

**Beenden**